

*“Science is a differential equation.
Religion is a boundary condition.”*

– Alan Turing



Module II: Computations in the Physical World, Lecture II.c

Chi-Ning Chou @ 2022 January Mini-Course “What is Computation? From Turing Machines to Black Holes and Neurons”

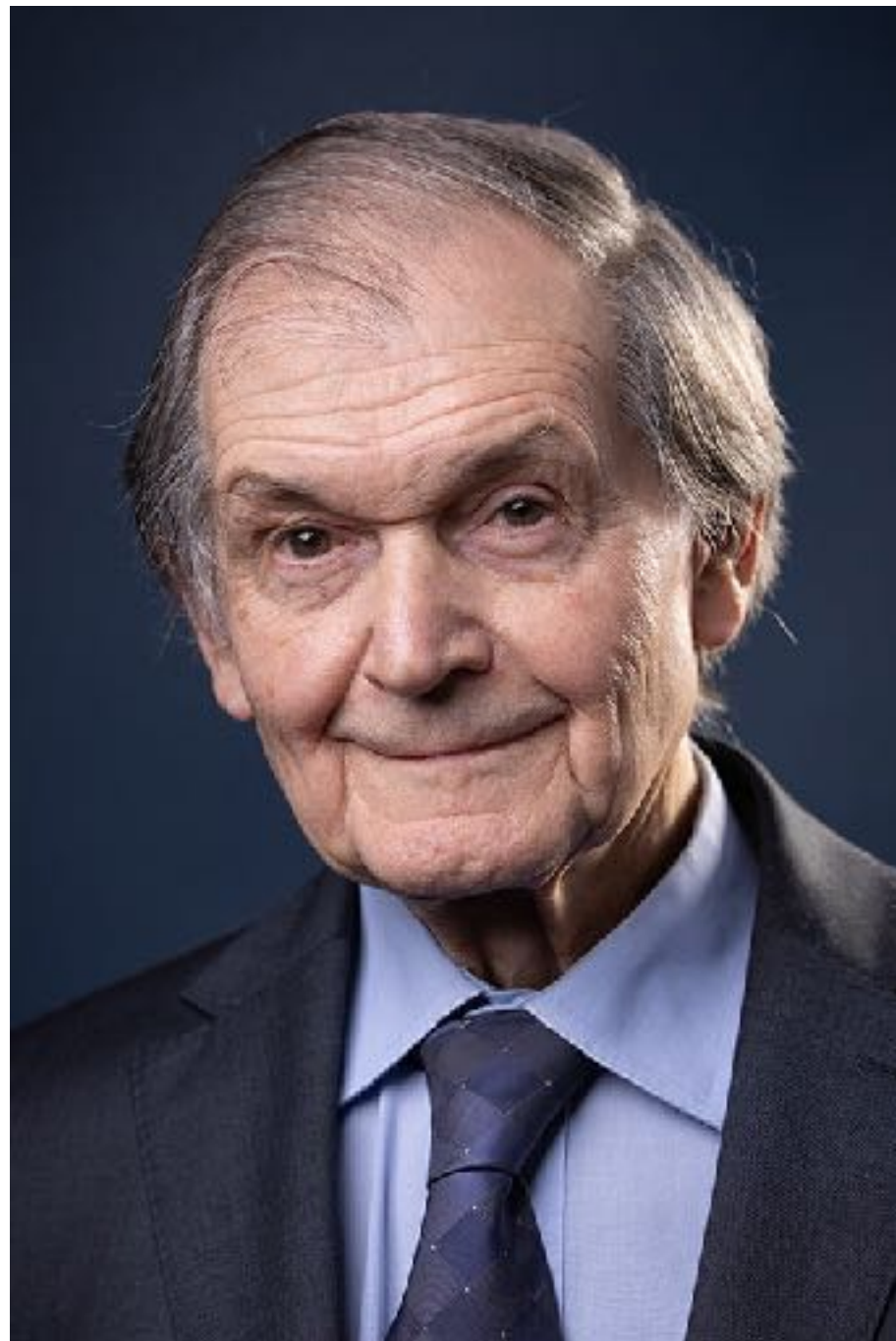
The Road to Reality: New Insights from Computation?

Module II: Computations in the Physical World

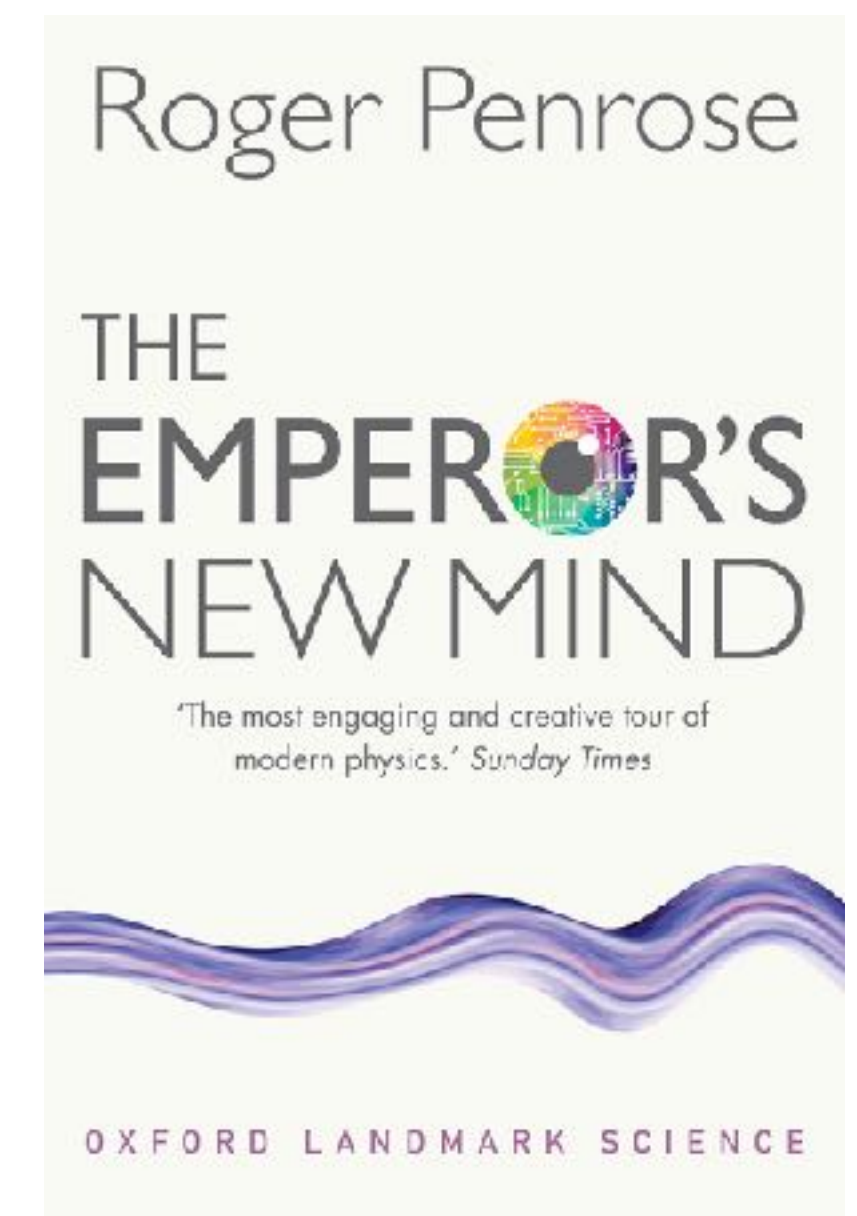
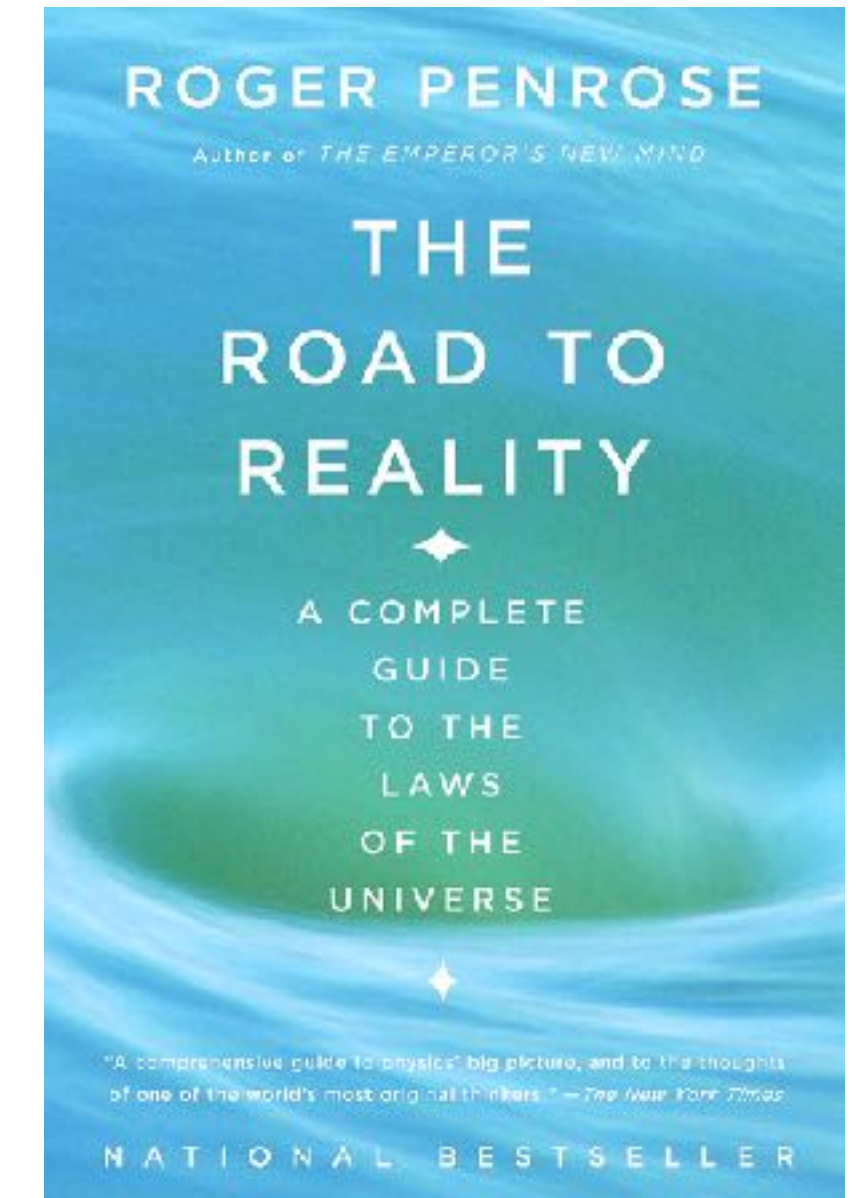
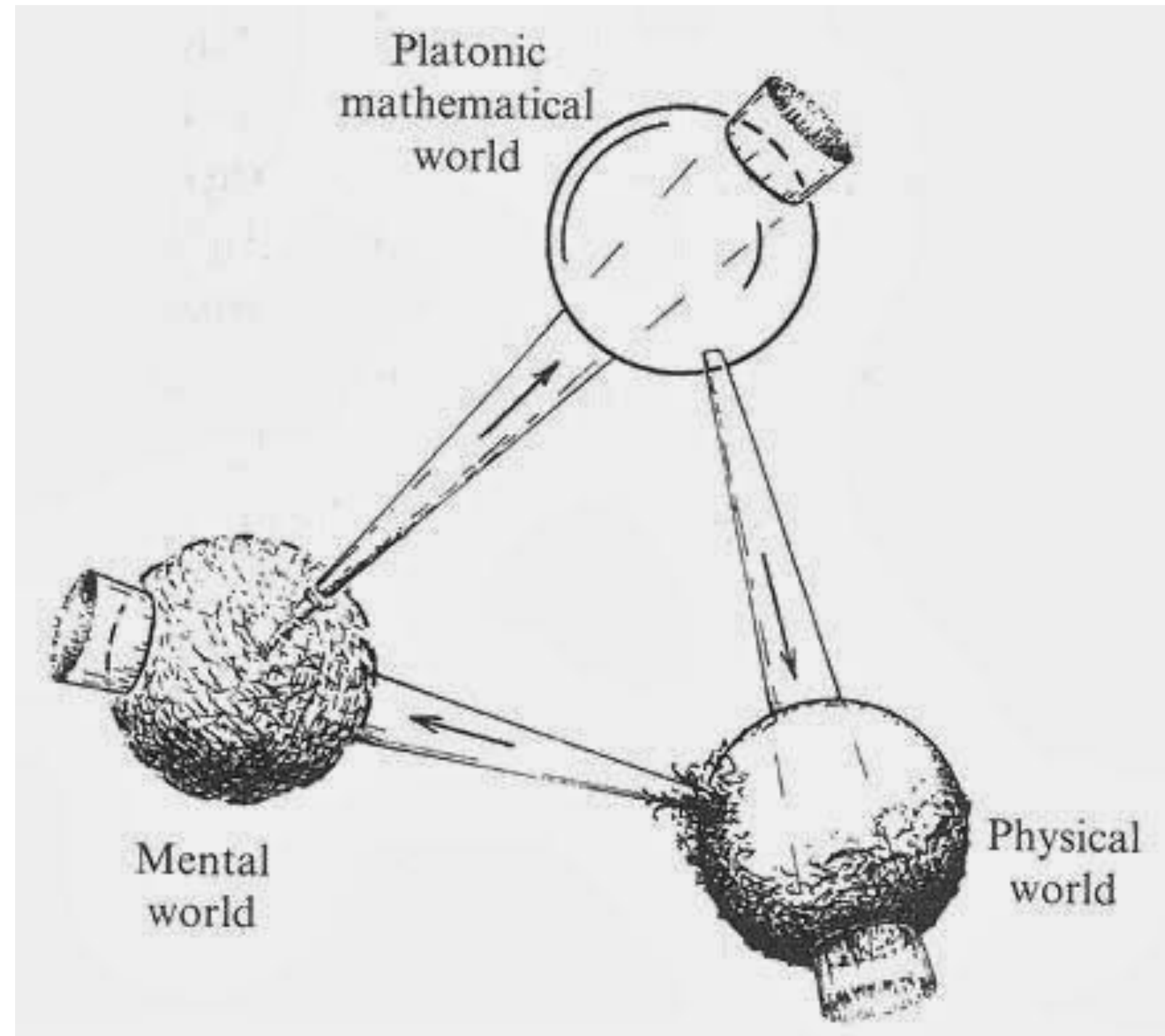
"Science is a differential equation. Religion is a boundary condition."

– Alan Turing

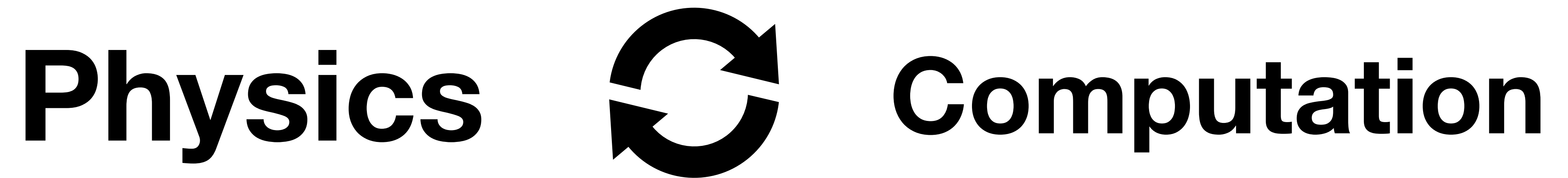
Penrose's Three Worlds



Roger Penrose
1931-present



What's the limitation of computation in the physical world?



How fundamental does computation play a role in the physical world?

Discrete vs. Continuous

Justin

If we agree that Physical World is doing Computation, we mostly use real or complex numbers for describing physical variables. However, Turing Machine is mapping integers to integers. How can Turing Machine capture all “Computation” if Physical World is doing Computation using real or complex numbers?

Digital
vs.
Analog

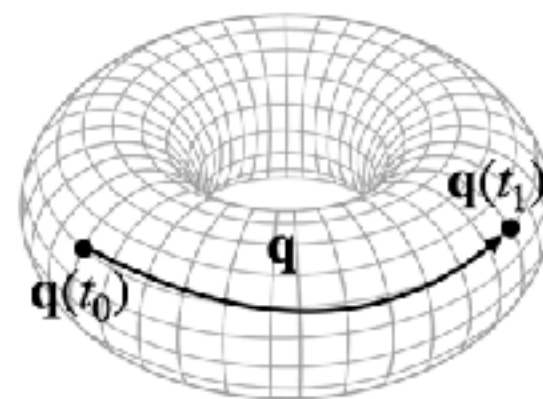
Real-Valued
Computational Models
(E.g., BSS machine)

Though the physical world
might be continuous, the
measurements are discrete
(i.e., Planck scale)!?

**How fundamental does computation
play a role in the physical world?**

Computation in the Physical World

Classical Mechanics as Optimization



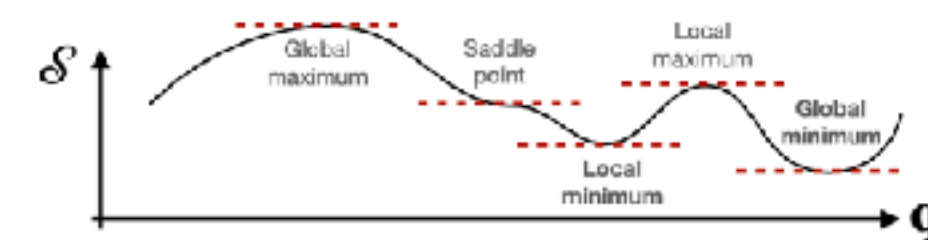
Principle of Stationary Action

The trajectory q will be the one that minimizes

$$\mathcal{S}[q] = \int_{t_0}^{t_1} L(q(t), \dot{q}(t), t) dt.$$

Principle of least action \Rightarrow

The physical reality locally minimizes the total action



Q: How to find the minimizer? **A:** Euler-Lagrange equations: $\frac{\partial L}{\partial q} = \frac{d}{dt} \frac{\partial L}{\partial \dot{q}}$.

15

* Here we focus on Lagrangian mechanics, other formulations (e.g., Hamiltonian mechanics) and more mathematical details will be covered in advanced sections.

Statistical Mechanics as Computation

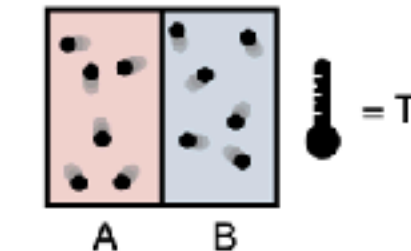
Optimization & Sampling & Counting



Simone
(Jan. 14
2pm-3pm ET)

"Simulated Annealing"

$$\Pr[\text{energy of } A = E] = \frac{\exp(-E/T)}{Z(T)}.$$



Optimization: Microstate with *lower* energy has higher probability!

Sampling: Start with a random microstate and lower the temperature.

Counting: The partition function $Z(T)$ encodes the number of microstates!

25

* More mathematical details in advanced sections.

Excitement in Quantum Computing!

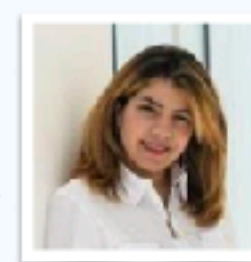
Be careful with the information, and make your own judgement!



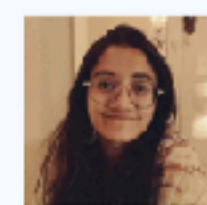
Xun Gao
(Jan. 13 11am-12pm ET)

"Quantum Correlation:
the Resource to Make
Quantum Machine
More Powerful"

"Quantum Machine
Learning from
Algorithms to Reality"



Khadijeh Sona Najafi
(Jan. 14 11am-12pm ET)



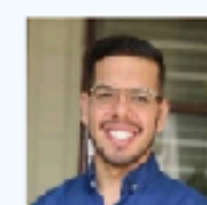
Sowmya
(Jan. 18
10am-11am ET)

"Basic of Quantum Computing
and Future Direction"



Avantika
(Jan. 18
11am-12pm ET)

"Quantum
Complexity Theory"



Kartikeya
(Jan. 20
9am-10am ET)

"Quantum Computing
from a Condensed
Matter Perspective"

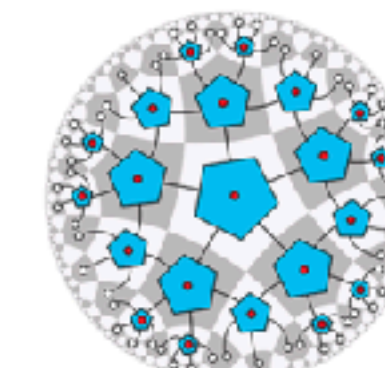
Computation as a New Angle for Gravity?

Black holes as...

Information Scramblers

Error-Correcting Codes

Black holes "look
very random"!?
(pseudorandom)

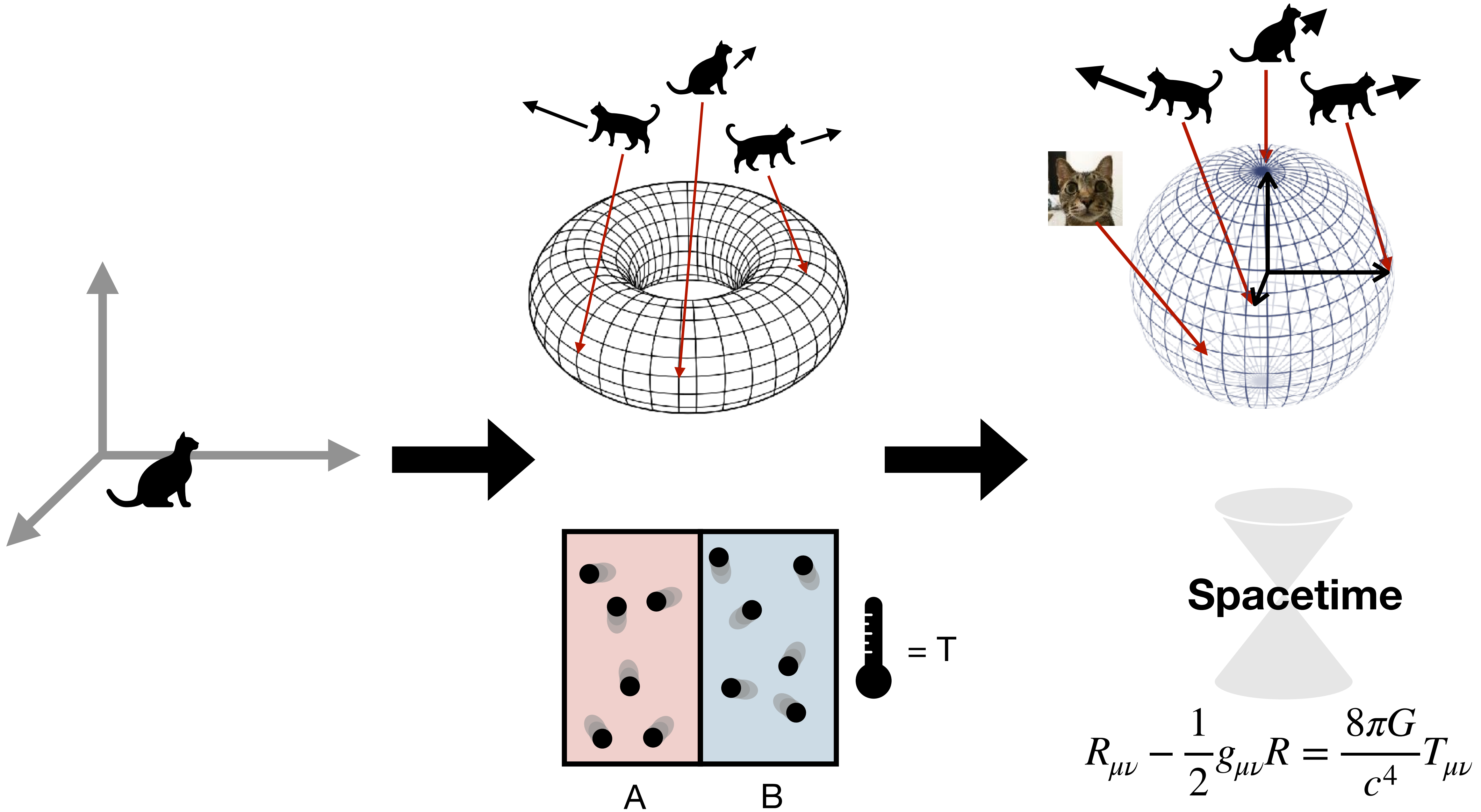


The interior of a
black hole can be
"locally decoded"!?

, and more...?

Properly explaining these requires some prerequisites, I might offer an advanced section on this if enough people are interested!

33



How Does a Physical System Compute?



Step 1: Encode the problem into the system

Step 2: Let the system evolve (unleash the power)

Step 3: Readout the output

How fundamental computation is in the physical world?

Consider the following thought experiment...

Q1: Does everything perform a certain computation? Or, does everything perform any computation? Is computation independent to particles, fields, forces, spacetime, etc.?

Q2: If all or some of the above were true, what does this mean? What's the difference between computation done by a physical system compared to the intuitive idea of “mechanical procedure”? What can the lens of computation bring to physics?

Type your thoughts in zoom chat!



Pancomputationalism (PC)

Unlimited PC

Everything can do every computation.

Limited PC

Everything can do some computation.

Ontic PC

The universe is a computing system.

My personal view:

- The issue of encoding problem.
- The statements seem to be vacuous, i.e., not much new insights yet?

We need to be more concrete and dig into it further!

What Insights Can Computation Give Us?

As physicists discover the importance of entropy, momentum, energy, etc....

What aspects of computation are analyzable and insightful?

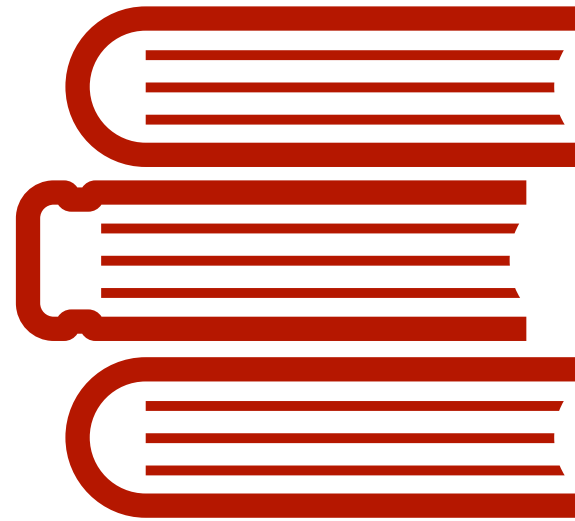
Maybe computational complexity could be a good candidate?

But it seems that complexity theorists cannot solve their own problems...

Maybe restricting ourselves to physically-relevant computations/algorithms can open the door!? E.g., in statistical physics, people do have exactly solvable models for certain realistic cases.

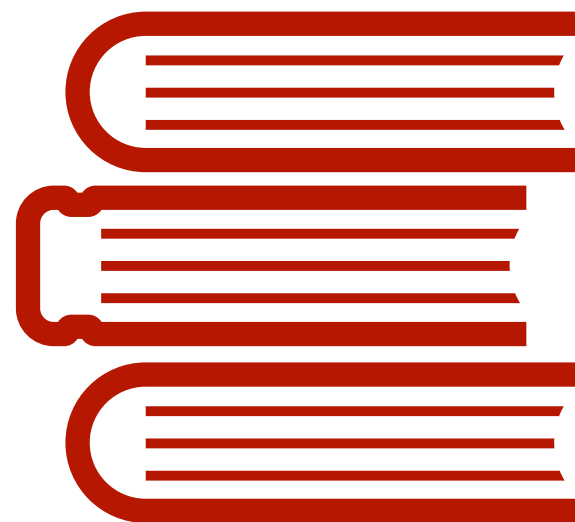
**What's the limitation of
computation in the physical world?**

Physical Church-Turing Thesis



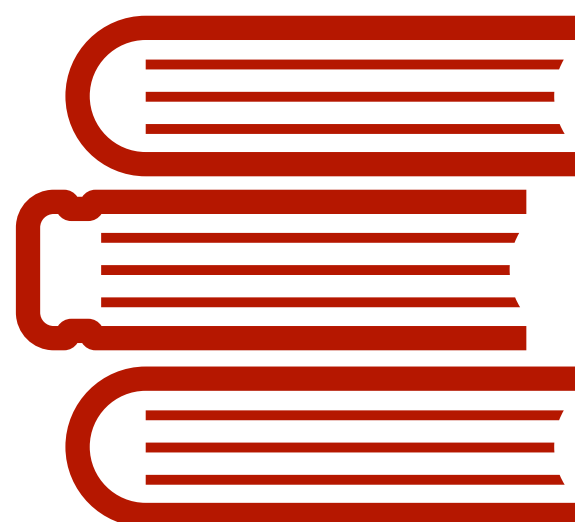
Mathematical Church-Turing Thesis

All **computable functions/numbers** can be computed by a Turing machine.



Physical Church-Turing Thesis

All **feasible** computation in the physical world can be done by a Turing machine.



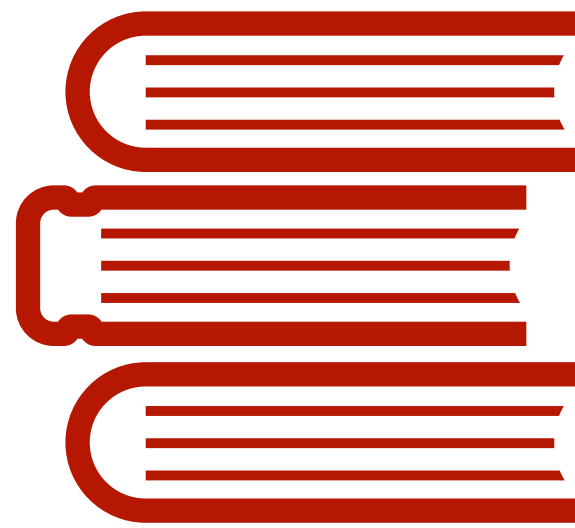
Extended Church-Turing Thesis

All **feasible** computation in the physical world can be done by a Turing machine **efficiently**.

Stronger



Can Turing Machine Simulate Classical Mechanics?



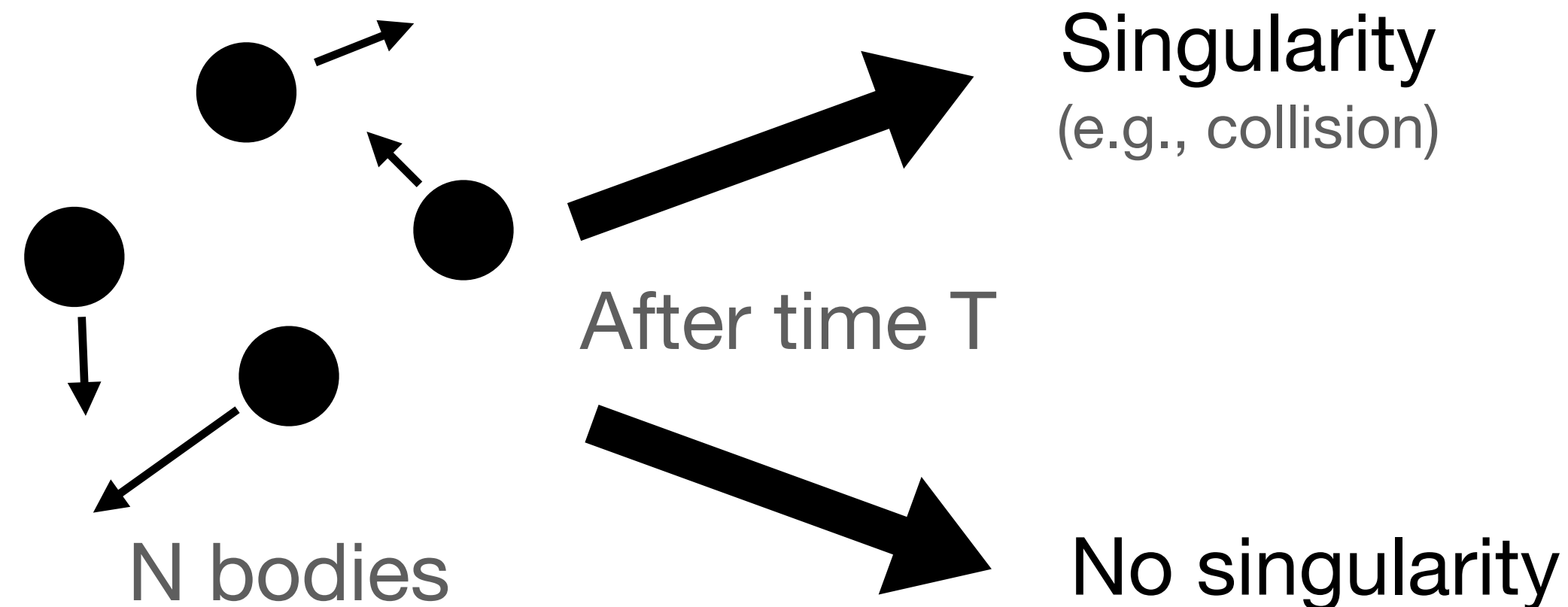
Extended Church-Turing Thesis

All **feasible** computation in the physical world can be done by a Turing machine **efficiently**.

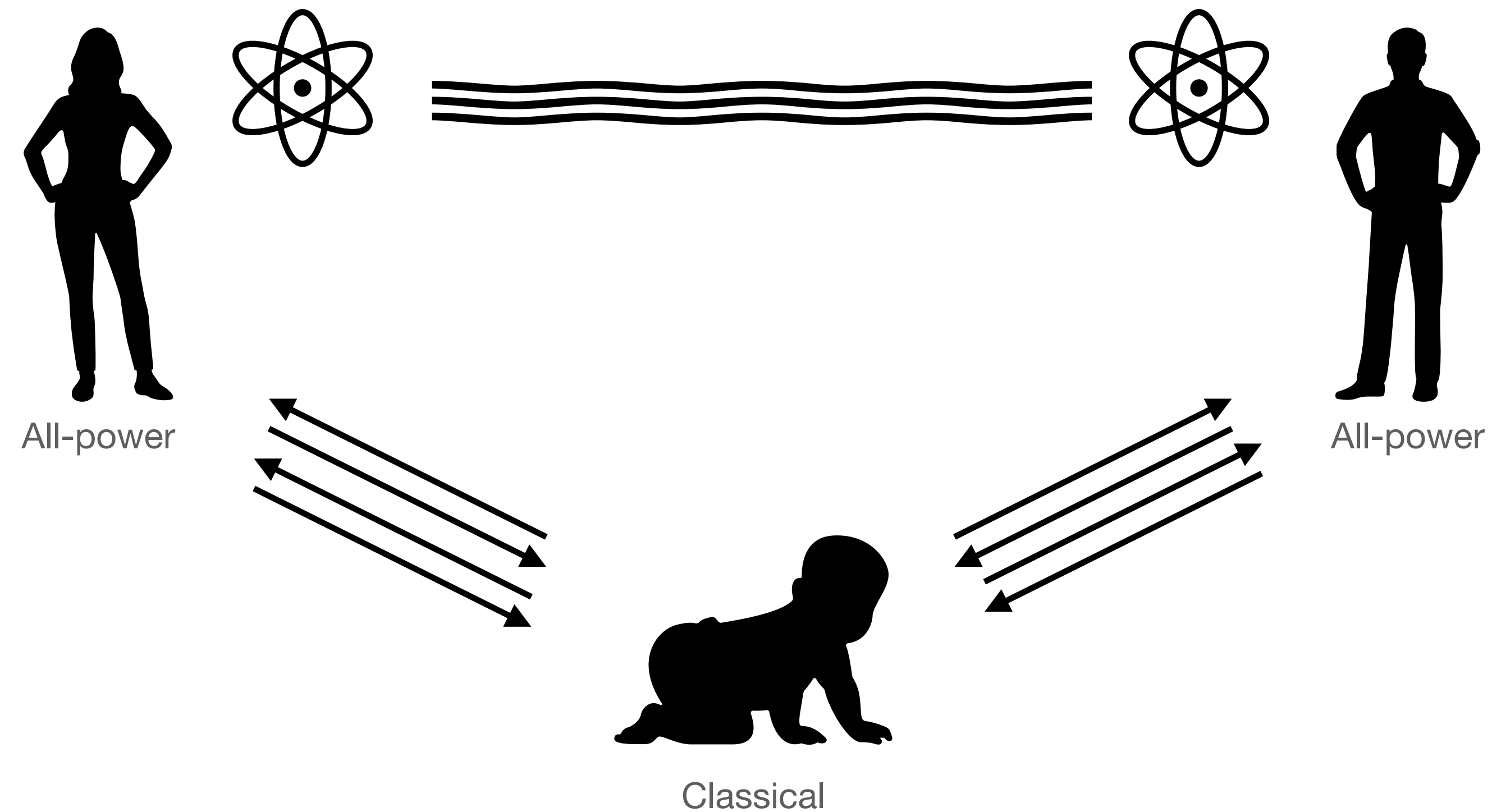
Q: Can we identify some computational problems in classical mechanics that cannot be efficiently computed by a Turing machine?



Andrew Chi-Chih Yao



$$\text{MIP}^* = \text{RE}$$



They can solve the Halting Problem in polynomial time!

How to interpret their results in the physical world?

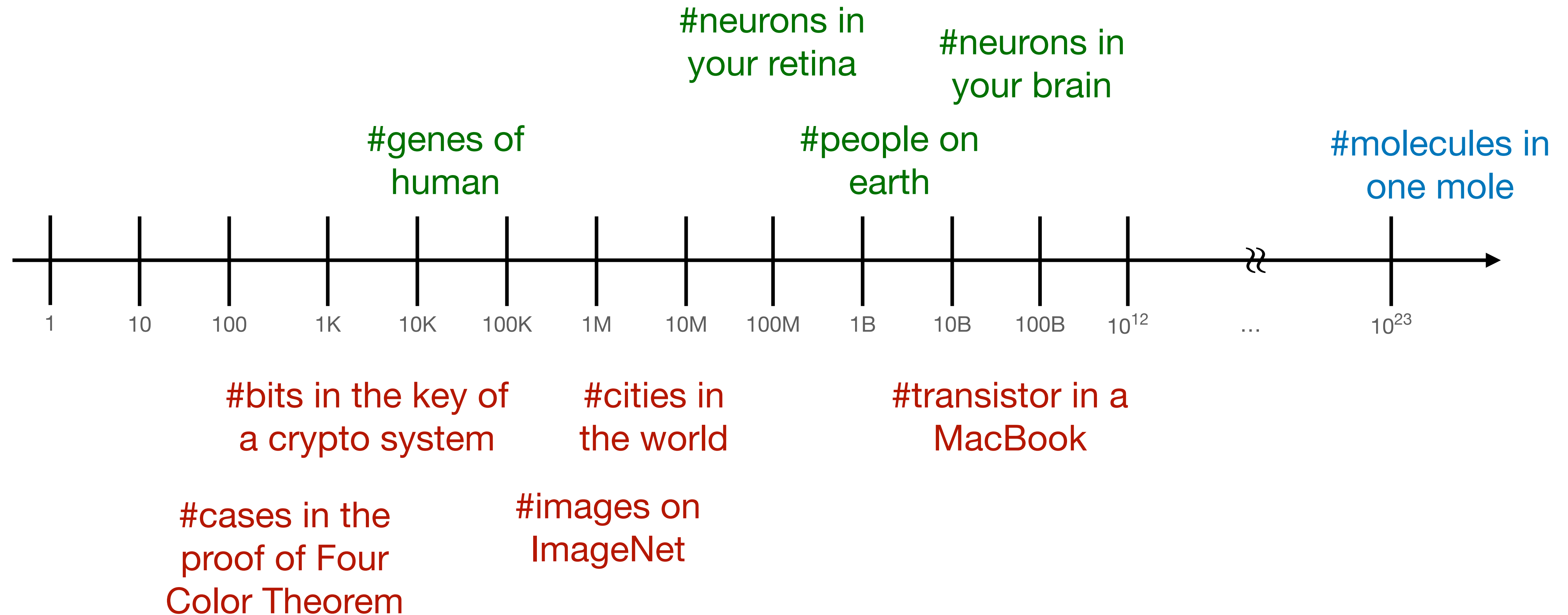
Limitations of Computation in the Physical World

Q3: How to interpret results like Shor's algorithm and $MIP^*=RE$ where the theoretical computational models haven't been implemented or even might not be able to be built?

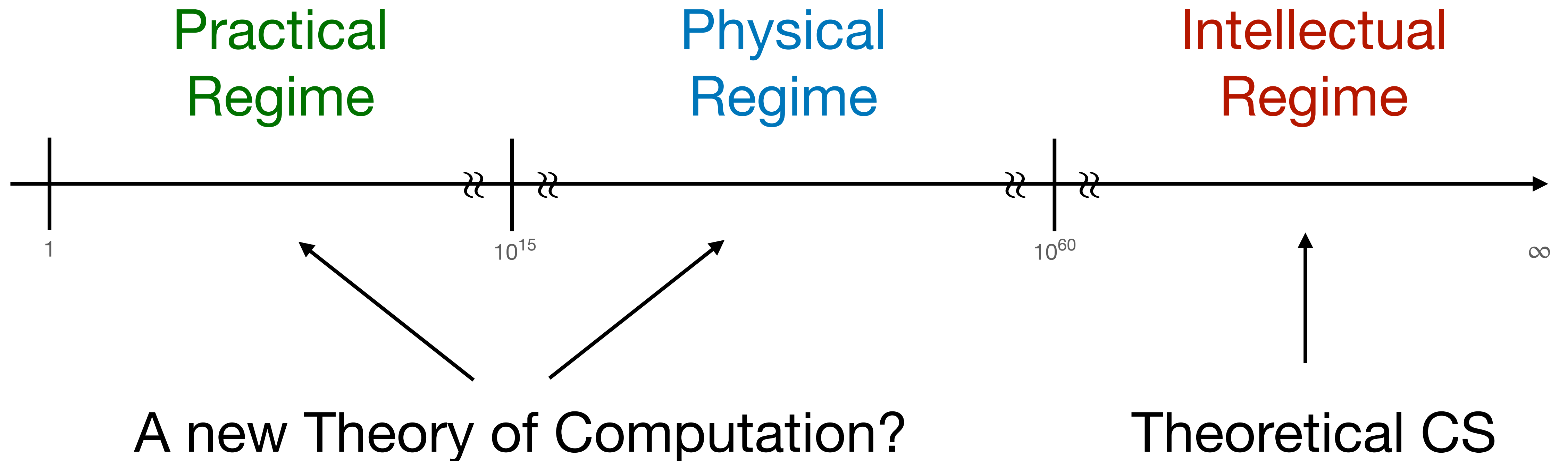
Q4: Infinity plays an important role in both theoretical physics and theoretical computer science. The former has a great success due to the fact that the order of atoms is indeed quite large (e.g., 10^{20}). However, the size of the computation problems we encounter in the real world could potentially be much smaller. What's your opinion on taking infinity/asymptotic into account when studying the computation in the physical world?

Type your thoughts in zoom chat!

Finiteness Matters!?



Three Regimes?



Summary

Questions of This Lecture

Q1: Does everything perform certain computation? Or, does everything perform any computation? Does computation prior to particles, fields, forces, spacetime, ...?

Q2: If some of the above were true, what does this mean? What's the difference between computation done by a physical system compared to the intuitive idea of “mechanical procedure”? What can the lens of computation bring to physics?

Q3: How to interpret results like Shor's algorithm and $MIP^*=RE$ where the theoretical computational models haven't been implemented or even might not be able to be built?

Q4: Infinity plays an important role in both theoretical physics and theoretical computer science. The former has a great success due to the fact that the order of atoms is indeed quite large (e.g., 10^{20}). However, the size of the computation problems we encounter in the real world could potentially be much smaller. What's your opinion on taking infinity/asymptotic into account when studying the computation in the physical world?

Next



Lecture III.c (Jan. 20 10am-10:50am ET)



Salvador
(Jan. 20
1pm-2pm ET)

*“Computing with Chemistry:
Turing Machines, Graph
Colouring, and DNA”*



Kartikeya
(Jan. 20
9am-10am ET)

*“Quantum Computing
from a Condensed
Matter Perspective”*



Chi-Ning
(Jan. 21
9am-10am ET)

*“When Black Holes Meet
Computational Complexity”*



Zhiqian Wang
(Jan. 19 11am-12pm ET)

*“A Road to Totality:
Between Art and
Computation”*

References

Articles:

- Yao, Andrew Chi-Chih. “Classical physics and the Church–Turing thesis.” Journal of the ACM (JACM) 50.1 (2003): 100-105, [link](#).
- Piccinini, Gualtiero and Corey Maley, “Computation in Physical Systems”, The Stanford Encyclopedia of Philosophy (Summer 2021 Edition), Edward N. Zalta (ed.), [link](#).

Introductory Books:

- Feynman, Richard P., Tony Hey, and Robin W. Allen. Feynman lectures on computation. CRC Press, 2018, [link](#).
- Penrose, Roger. The road to reality: A complete guide to the laws of the universe. Random house, 2005, [link](#).
- Mezard, Marc, and Andrea Montanari. Information, physics, and computation. Oxford University Press, 2009, [link](#).

Advanced Books:

- Mézard, Marc, Giorgio Parisi, and Miguel Angel Virasoro. Spin glass theory and beyond: An Introduction to the Replica Method and Its Applications. Vol. 9. World Scientific Publishing Company, 1987, [link](#).
- Sakurai, Jun John, and Eugene D. Commins. “Modern quantum mechanics, revised edition.” (1995): 93-95, [link](#).